

NEUB Fall 2018 CSE 431: Digital Signal Processing Test 01 Set A

Answer all the questions.

Total Mark: 10

Total Time: 25 Minutes

- Is the system a. $y(t) = x^3(t)$ and b. $y(t) = ax(t) + 2$ Linear, Time-Invariant, Continuous-time? [3]
 - $y(t) = x^3(t) \rightarrow$ Not linear, Time invariant, continuous
 - $y(t) = ax(t) + 2 \rightarrow$ Not linear, Time invariant, continuous
- Explain the difference between Even and Odd Signal. [2]

A continuous signal is

Even if $x(-t) = x(t)$ for all values of x

Odd if $x(-t) = -x(t)$ for all values of x

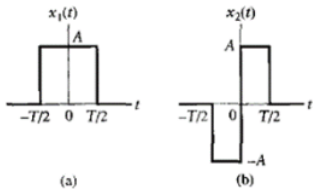
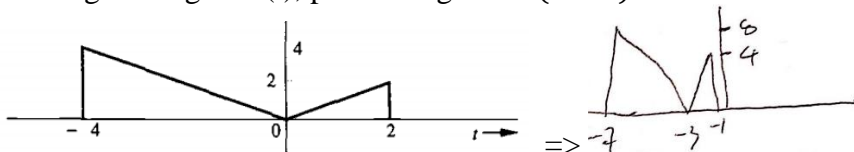
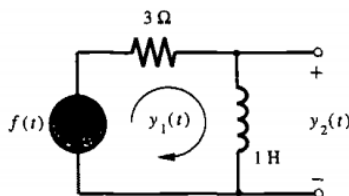


Figure 6 (a) Even Signal (b) Odd signal

- For the given signal $x(t)$, plot the signal $2x(t + 3)$. [2]



- For the circuit depicted in figure below, find the differential equations relating the outputs $y_1(t)$ and $y_2(t)$ to the input $f(t)$. [3]



Handwritten solution for the circuit problem:

$V_L = L \frac{di}{dt}$
 $V_R = iR$
 hence $I = y_1$
 $V_L = y_2(t)$
 So $y_2(t) = 1 \frac{d}{dt} y_1(t)$
 $= \frac{d}{dt} y_1(t)$
 $= D y_1(t)$
 or $y_1(t) = \frac{1}{D} y_2(t)$

For $f(t)$ & $y_1(t)$
 $f(t) = 3 y_1(t) + 1 \times \frac{d}{dt} y_1(t)$
 $f(t) = 3 y_1(t) + D y_1(t)$
 $f(t) = (3 + D) y_1(t)$ //

For $f(t)$ & $y_2(t)$
 $f(t) = 3 y_1(t) + \frac{d}{dt} y_1(t)$
 $f(t) = \frac{3}{D} y_2(t) + y_2(t)$

$D f(t) = 3 y_2(t) + D y_2(t)$
 $D f(t) = (3 + D) y_2(t)$ //

NEUB Fall 2018 CSE 431: Digital Signal Processing Test 01 Set B

Answer all the questions.

Total Mark: 10

Total Time: 25 Minutes

- Is the system a. $y(t) = \sin(x(t))$ and b. $y(t) = x^2(t)$ Linear, Time-Invariant, Continuous-time? [3]
 - $y(t) = \sin(x(t)) \rightarrow$ Not linear, Time invariant, continuous
 - $y(t) = x^2(t) \rightarrow$ Not linear, Time invariant, continuous
- Explain the difference between energy signal and power signal. [2]
A signal with finite energy is an energy signal, and a signal with finite and nonzero power is a power signal.

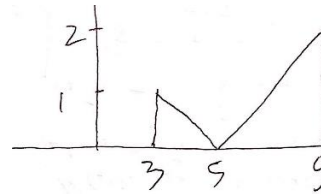
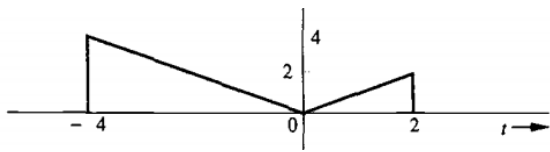
Energy of a signal can be found by the formula

$$E_f = \int_{-\infty}^{\infty} f^2(t) dt$$

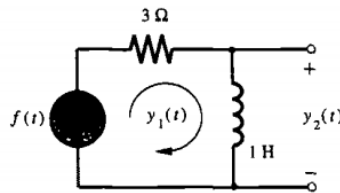
The definition can be generalized to a complex valued signal $f(t)$ as

$$E_f = \int_{-\infty}^{\infty} |f(t)|^2 dt$$

- For the given signal $x(t)$, plot the signal $\frac{1}{2}x(-5-t)$. [2]



- For the circuit depicted in figure below, find the differential equations relating the outputs $y_1(t)$ and $y_2(t)$ to the input $f(t)$. [3]



Handwritten solution for the circuit problem:

For $f(t)$ & $y_1(t)$

$$f(t) = 3y_1(t) + 1 \times \frac{\partial}{\partial t} y_1(t)$$

$$f(t) = 3y_1(t) + D y_1(t)$$

$$f(t) = (3 + D) y_1(t) //$$

For $f(t)$ & $y_2(t)$

$$f(t) = 3y_2(t) + \frac{\partial}{\partial t} y_2(t)$$

$$f(t) = \frac{3}{D} y_2(t) + y_2(t)$$

$$D f(t) = 3y_2(t) + D y_2(t)$$

$$D f(t) = (3 + D) y_2(t) //$$

Additional notes:

$V_L = L \frac{di}{dt}$
 $V_R = iR$
 here $I = y_1(t)$
 $V_L = y_2(t)$
 So $y_2(t) = \frac{\partial}{\partial t} y_1(t)$
 $= \frac{\partial}{\partial t} y_1(t)$
 $= D y_1(t)$
 $\Rightarrow y_1(t) = \frac{1}{D} y_2(t)$